

# Transition vers la cryptographie post-quantique

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# What can quantum computers do?

General-purpose quantum computers can run **quantum algorithms** including

1. **Shor's algorithm** (1991)

- Uses the **quantum Fourier transform** to efficiently detect cycle periods
- Solves integer factorization and discrete logarithm problems in **polynomial time**

2. **Grover's quantum search algorithm** (1996)

- Searches an unstructured set of  $N$  items in time  $\sim \sqrt{N}$
- Classical computers need time  $\sim N$  for the same task

# When will quantum computers arrive?

**When?** For the last 15 years, the answer is typically “**probably in 10 years**”.

Constructing general-purpose quantum processors is a massive challenge for **experimental physics** and **engineering**.

So far: incremental progress.

**Shor’s algorithm:** current (public) record for **integer factorization** is  $21 = 3 \times 7$  (in 2012! with 10 qubits)

Progress: IBM announced a 433-qubit machine in 2022.<sup>1</sup>

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<sup>1</sup>Source: IBM. Analysis: Olivier Ezratty

# Quantum resources

Estimates<sup>2</sup> of actual quantum resources (logical qubits, gates/operations) required to break basic asymmetric cryptography using Shor's algorithm:

Security level	Security (bits)	RSA/Factoring			Elliptic Curve Discrete Log		
		Key bits	Qubits	Operations	Key bits	Qubits	Operations
<i>Legacy</i>	80-bit	1024	2050	$5.81 \times 10^{11}$	160	1466	$2.97 \times 10^{10}$
<i>Reduced</i>	112-bit	2048	4098	$5.20 \times 10^{12}$	224	2042	$8.43 \times 10^{10}$
<i>Basic</i>	128-bit	3072	6146	$1.86 \times 10^{13}$	256	2330	$1.26 \times 10^{11}$
...	192-bit	7680	15362	$3.30 \times 10^{14}$	384	3484	$4.52 \times 10^{11}$
<i>Paranoid</i>	256-bit	15360	30722	$2.87 \times 10^{15}$	512	4719	$1.14 \times 10^{12}$

<sup>2</sup>Source: BSI Quantum-safe cryptography (2021)

Post-quantum cryptosystems are designed to

- run on today's **conventional hardware**,
- resist** future conventional adversaries, and
- resist** future adversaries with powerful **quantum computers**.

Aim: upgrade the crypto in everyday security protocols and products to add quantum-safety.

*This has essentially nothing to do with **quantum cryptosystems** (e.g. QKD), which run on quantum devices and channels, and not on conventional hardware.*

# Post-quantum cryptography: when?

Cryptographers are already developing post-quantum cryptosystems.

When should we **transition** to using them?

Transition has to begin **now**.

- Long-term data privacy: adversaries can store now, decrypt later
- Long-term infrastructure: e.g. root certificates can have ten-year lifetimes

**Symmetric cryptography:** data privacy (encryption) and authenticity (MACs).

**Postquantum symmetric cryptography** is mostly a reaction to **Grover's algorithm**, which allows “brute-force” search in square-root time. *For example:*

- find  $n$ -bit **encryption keys** in  $2^{n/2}$  operations instead of  $2^n$
- find **preimages** of  $n$ -bit hashes in  $2^{n/2}$  operations instead of  $2^n$ .

**Basic response:** double existing symmetric key/hash lengths.

# Quantum-safe data encryption

Transition case study: **data encryption**.

- **Today:** we use standard **AES-128** (128-bit keys).
- **Quantum safety:** switch to standard AES-256 (256-bit keys).
- **Deployment:** AES-256 is already widely deployed.
- **Confidence:** AES-256 is already a long-term standard, 20 years of analysis
- **Practical consequences:**
  - Key management/storage requirements double
  - Encrypted data: same size
  - Speed and energy: 25-30% performance hit

**Conclusion:** transition is relatively **manageable**.



# Asymmetric/Public-key cryptography in 2022

Asymmetric (public-key) cryptography: fundamental tasks are

Objective	Deployed systems
<b>Key agreement</b> <i>Prior to symmetric encryption</i>	Elliptic-curve Diffie–Hellman, RSA key agreement
<b>Signatures</b> <i>Authentication and identification</i>	RSA signatures, ECDSA, Ed25519

Virtually all deployed systems depend on the hardness of factoring or discrete logs, so are **totally broken by Shor's algorithm**.

**NIST** (US National Institute of Standards and Technology) has a **post-quantum standardization project** to select quantum-safe key agreement and signatures.

## NIST Round 3 and 4 KEM parameters

Key agreement at today's basic 128-bit security level (NIST Level 1):

	Candidate	Paradigm	Public key	Ciphertext
<i>"Pre-quantum"</i>	X25519	ECC	32 B	32 B
<b><i>New Standard</i></b>	<b>Kyber512</b>	<b>Lattice-based</b>	<b>800 B</b>	<b>768 B</b>
<i>Future standardization candidates</i>	ClassicMcEliece384464	Code-based	261120 B	128 B
	BIKE	Code-based	1540 B	1572 B
	HQC-128	Code-based	2249 B	4481 B

- Post-quantum key agreements can often run **faster**, but
- they have **much larger** public keys and bandwidth requirements, and
- can present new challenges for secure implementation  
(*more memory, more randomness, side-channel defences, ...*)

## NIST Round 3 Signature parameters

**Signatures** at today's basic 128-bit security level (NIST Level I):

	Candidate	Paradigm	Public key	Signature
<i>"Pre-quantum"</i>	Ed25519	ECC	32 B	64 B
<b><i>New standards</i></b>	Dilithium (Level II)	Lattice-based	1312 B	2420 B
	Falcon-512	Lattice-based	897 B	666 B
	SPHINCS+-128s	Hash-based	32 B	7856 B
	SPHINCS+-128f	Hash-based	32 B	17088 B

Quantum-safe signatures typically have **much larger keys and signatures**.

"Round 4": NIST is requesting new alternative signature schemes based on other hard problems.

# Post-quantum transition; asymmetric crypto

In **theory**, we know what to do: replace ECC and RSA post-quantum standards.

In **practice**, this is a massive real-time scientific experiment:

- **Real-world performance** needs much more study  
*e.g. large signatures may need two frames  $\implies$  network performance hit*
- **Low confidence**: new standards are immature, have faced less analysis
- **Side-channel attacks**: a **much larger attack surface** for timing attacks, power analysis, ...
- Improved attacks may imply rapid **parameter changes** to maintain security
- Very few existing **implementations**:
  - **software**: optimizations and potential flaws both poorly understood
  - **hardware**: starting from scratch with a long development cycle

# Who is working on post-quantum cryptography

Large, high-profile French participation in post-quantum crypto research and standardization (NIST, IETF, IEEE, ...)

**Inria teams** include

- GRACE (Saclay + Campus Cyber)
- COSMIQ (Paris)
- CAPSULE (Rennes)
- ARIC (Lyon)

Also academic teams in Paris, Limoges, Caen, ...

**Companies** dedicated to post-quantum crypto include CryptoNext, PQShield, ...

## Strategic conclusions: What to do?

When planning your migration to post-quantum cryptography,

1. Follow the **standards** (of course!)
2. Insist on **crypto-agility** (easy modular switching between cryptosystems) to ease inevitable changes as standards evolve
3. Insist on **hybrid solutions** (pre- *AND* post-quantum) until new cryptosystems and software/hardware implementations mature

There are **post-quantum cryptography experts** all around you, don't hesitate to reach out!